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A Theory of Cash Flow-Based Financing with Distress Resolution

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We develop a dynamic contracting theory of asset- and cash flow-based financing that demonstrates how firm, intermediary, and capital market characteristics jointly shape firms' financing constraints. A firm with imperfect access to equity financing covers financing needs through costly sources: an intermediary and retained cash. The firm's financing capacity is endogenously determined by either the liquidation value of assets (asset-based) or the intermediary's going-concern valuation of the firm's cash flows (cash flow-based). The optimal contract is implemented with defaultable debt — specifically unsecured credit lines and senior-secured debt — and features risk-sharing via bankruptcy. When the firm does well, it repays its debt in full. When it does poorly, distress resolution mirrors U.S. bankruptcy procedures (Chapter 7 and 11). Secured and unsecured debt are complements because risk-sharing via unsecured debt increases secured debt capacity. Debt and equity are dynamic complements because future access to equity financing increases current debt capacity.

Keywords: Risk Management, Security Design, Optimal Contracting, Liquidity Management, Financing Capacity, Bankruptcy, Chapter 7, Chapter 11.

JEL Codes: G32, G35, G20, D86.

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1. INTRODUCTION

Financing constraints lead firms to manage liquidity risks with internal sources, such as retained earnings, and external sources, such as credit lines. At the same time, the total amount of external liquidity available to the firm depends on financing constraints. Specifically, it depends on the valuation of the firm as a collateral asset from the perspective of a financier who provides that external liquidity. If the financier values the firm's cash flows more than the liquidation value of the firm's assets, then it will extend liquidity based on this going-concern value of those cash flows, generating a distinction

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between asset-based and cash flow-based financing [\(Lian and Ma,](#page-32-0) [2021\)](#page-32-0). Consequently, the key determinant of financing constraints becomes the financier's valuation of the firm in distress, which depends on the firm's future financing arrangements and constraints.

This paper sheds light on the joint determination of financing constraints, the optimal management of liquidity risks, and distress resolution by presenting a theory of corporate finance based on dynamic risk sharing. Our main contribution is to show how defaultable debt and bankruptcy procedures emerge as optimal liquidity risk management tools that facilitate cash flow-based financing within a complete contracts framework. Specifically, our model endogenously generates distress resolution for optimal risk sharing that resembles bankruptcy procedures such as Chapter 7 and Chapter 11, linking the dynamics of bankruptcy to asset- versus cash flow-based financing. Our theory also highlights how debts of different seniority as well as debt and equity can act as complements in a firm's capital structure.

The optimal contract features dynamic risk sharing between the firm's constrained owners and an intermediary who provides liquidity at a cost. We show that a capital structure consisting of equity, senior-secured short-term debt (or credit line), and an unsecured credit line implements the optimal contract. The firm's secured debt capacity coincides with the intermediary's valuation of the firm as a collateral asset, which is either asset- or cash flow-based. Under this capital structure, resolving financial distress involves default on unsecured debt, while secured debt is repaid in full. Notably, default need not coincide with the liquidation of the firm's assets. In some cases, unsecured debt absorbs risk by taking a write-down—a form of default—during distress resolution, which allows the firm to avoid liquidation. This can raise the secured debt capacity of the firm today above its liquidation value and thereby facilitate cash flow-based financing. Thus, unsecured and secured debt are complements.

In more detail, we model a firm that produces risky cash flows and has imperfect access to capital markets. The firm's current owners cannot inject cash into the firm but, as in [Hugonnier et al.](#page-32-1) [\(2015\)](#page-32-1), the firm can raise external financing at intermittent random times from new competitive, risk-neutral investors who subsequently become hand-to-mouth. Such intermittent access to broader and competitive capital markets captures capital supply risk. An intermediary stands ready to provide liquidity at any time. Thus, absent market access, the firm finances cash flow shortfalls, i.e., manages liquidity risks, with internal cash reserves and/or funds provided by the intermediary. However, both liquidity facilities are costly. First, cash held in the firm earns a return below the risk-free rate. Second, the intermediary requires compensation for exposure to risk which reflects its own financial or regulatory constraints, limiting its risk-bearing capacity.

We derive the optimal contract under commitment between the firm's owners and the intermediary that maximizes firm value. In the optimal contract, the firm's owners act as shareholders and the firm raises new equity upon capital market access. The intermediary provides liquidity between equity financing rounds. As we show, its claim resembles defaultable debt, so the intermediary may represent a bank or a non-bank lender.

We can summarize the firm's state with a single variable that we term net liquidity. Because the firm has infrequent access to equity financing, negative cash flow shocks reduce net liquidity and can induce financial distress, making the firm's shareholders effectively risk-averse. As such, it becomes optimal to share liquidity risks, in the form of cash flow and capital supply risks, with the intermediary. Specifically, the intermediary bears a fraction of cash flow risk that increases as net liquidity decreases.

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The intermediary also provides financing to the firm in exchange for a payout in the next equity financing round. However, because the firm's current shareholders cannot inject funds into the firm, the maximum payout that can be promised to the intermediary equals the total resale value of the firm during an equity financing round.

The shareholders' value function solves an ordinary differential equation with two free boundaries. At the upper boundary the firm pays dividends to its shareholders. At the lower boundary, either the firm is liquidated or the intermediary provides the necessary financing to facilitate continuation. When the intermediary values the firm below its liquidation value, financing capacity is asset-based, i.e., determined by the exogenous liquidation value of the firm's assets, and hitting the lower boundary results in liquidation. Otherwise, it is cash flow-based, i.e., determined by the intermediary's endogenous going-concern valuation of the firm's cash flows, consisting of two components. The first is the exogenous risk-adjusted value of the cash flows it will receive prior to selling the firm to new investors upon capital market access. The second component is the expected discounted proceeds from selling the firm to new investors at the fair market value, which endogenously depends on future liquidity risk management and thus on the contract with the intermediary. This second effect means that more efficient risk sharing and, specifically, distress resolution, both in the present and the future, increases cash-flow based financing capacity.

Once the firm exhausts its financing capacity, i.e., when net liquidity approaches its lower boundary, the intermediary effectively takes full ownership of the firm while existing shareholders are wiped out. If financing capacity is cash flow-based, the intermediary bears all liquidity risk and allows the firm to continue operations until it can sell the firm to new investors. In contrast, when financing capacity is asset-based, the intermediary liquidates the firm. Thus, the nature of financing capacity shapes the resolution of financial distress and vice versa. If the intermediary anticipates that the firm will optimally resolve distress without liquidation in the future, it is willing to provide cash flow-based financing today, which in turn facilitates distress resolution without liquidation.

To implement this contract via standard securities, we first show that the sum of past transfers to and from the intermediary since last market access, compounded at an endogenous rate, is a sufficient statistic for the contract's state. We interpret this sum as the balance of a credit line because it accumulates past transfers, i.e., drawdowns and repayments, and accrued interest, with its balance due upon market access.

Current shareholders raise equity to replenish the cash balance of the firm upon market access, creating value in the process. They also a make payment to the intermediary that resets the credit line balance to zero. If the balance of the credit line is small, then the value of the firm to the new equity investors is high and the firm raises enough cash to achieve the target cash balance, pay off the credit line in full, and allow existing shareholders to maintain a stake in the firm. However, if the balance of the credit line is large, there is insufficient value to achieve all three objectives. The contract then forces the current shareholder to raise the most cash they can by selling their entire stake in the firm. In order to create maximal value, the proceeds are first used to achieve the target cash balance. The remaining proceeds are allocated to the intermediary, and even though they are less than the credit line balance, the balance is reset to zero. Effectively, raising new equity when the firm is in financial distress wipes out existing shareholders and leads to partial default on the credit line.

This repayment schedule is consistent with an absolute priority rule in which the intermediary must be repaid in full before the current shareholders and thus leads to the

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interpretation of the intermediary's claim as debt. As current shareholders are worse off by raising new equity when the outstanding debt is large, the implementation features a debt overhang problem. To overcome this problem, we allocate control rights in distress states to the intermediary that allow it to force a sale of the firm in case of market access.

The optimal contract involves two key elements, financing against promised repayments and risk sharing. To better delineate these functions, we further split the intermediary's claim into senior-secured and unsecured debt. Senior-secured debt or, in short, secured debt, is always repaid in full; it can be implemented as short-maturity term debt or a credit line. The firm's capacity for this form of debt coincides with the intermediary's valuation of the firm as a collateral asset. In contrast, unsecured debt features default in distress states and takes the form of a credit line. The unsecured credit line is used as a liquidity risk management tool over the entire state space. It facilitates risk-sharing with the intermediary because it features default in some states. The secured debt is used to finance cash flow shortfalls once the firm has run out of cash. It does not implement any risk-sharing but merely provides financing against promised future repayments because it earns the market interest rate and is always fully repaid.

The optimal contract resolves financial distress in a manner resembling US bankruptcy procedures. A debt covenant allocates control rights during distress to the creditors, i.e., the intermediary. Without this covenant, the current shareholders would not agree to raise more equity due to debt overhang. When the firm raises new equity outside of distress, it repays all creditors and existing shareholders are better off. Otherwise, the threat of bankruptcy enforces repayment of debt as long as the proceeds from raising equity are sufficient. If it is not possible to fully repay debt, creditors force Chapter 11 bankruptcy while the firm continues operations. Bankruptcy resolution follows one of three cases. First, upon finding new equity investors, the firm repays secured debt, partially defaults on unsecured debt, and wipes out existing equity claims. Second, while in Chapter 11, it may exhaust its financing capacity after a series of negative cash flows. The firm then converts to Chapter 7 and liquidates assets, repays secured debt, and wipes out unsecured debt and existing equity claims. Third, it may emerge from bankruptcy after a series of positive cash flows.

Our model highlights a novel mechanism that links asset- and cash flow-based financing to the mode of bankruptcy. Liquidation and conversion to Chapter 7 bankruptcy might occur under asset-based financing. In contrast, under cash flow-based financing, the firm never exhausts its financing capacity and eventually recovers from Chapter 11 bankruptcy by either locating new investors or earning its way out. Because creditors anticipate this scenario, they are willing to provide secured debt exceeding the liquidation value of assets, which as previously stated facilitates distress resolution without liquidation. Crucially, bankruptcy involves allocating risks to shareholders and unsecured creditors, which insures secured debt and allows access to it in distress.

Finally, our theory highlights how different financing instruments interact in the capital structure. First, unsecured and secured debt are complements. The unsecured credit line allows the firm to share risk with creditors, which can raise the collateral value of the firm. Specifically, by absorbing risk and staving off liquidation in distress, unsecured debt can ensure the repayment of secured debt even when its balance exceeds the liquidation value of assets. This relation allows cash-flow based financing. Second, debt and equity are dynamic complements. Improved access to equity financing increases the likelihood that debt is repaid and raises secured debt capacity, again facilitating cash flow-based financing. Third, our implementation features an overlapping pecking order in which unsecured debt is used in all states, while senior-secured debt is used only when

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out of cash. When the firm holds cash, it finances cash flow shortfalls with cash reserves and the unsecured credit line. When out of cash, it finances such shocks with both the unsecured credit line and secured debt.

Related Literature. Our paper relates to the literature on corporate liquidity and risk management, as exemplified by [Bolton et al.](#page-31-0) [\(2011\)](#page-31-1) and Décamps et al. (2011). [Bolton et al.](#page-31-0) [\(2011\)](#page-31-0) demonstrate how liquidity management and firm financing interacts with a firm's investment decisions. [Bolton et al.](#page-31-2) [\(2021\)](#page-31-2) study optimal debt issuance and investment when equity financing is costly. Further contributions in this literature include [Gryglewicz](#page-32-2) [\(2011\)](#page-32-2); [Bolton et al.](#page-31-3) [\(2013\)](#page-31-3); Décamps et al. [\(2016\)](#page-31-4); [Hugonnier and](#page-32-3) [Morellec](#page-32-3) [\(2017\)](#page-32-3); [Malamud and Zucchi](#page-32-4) [\(2018\)](#page-32-4), and, more recently, [Abel and Panageas](#page-31-5) [\(2023\)](#page-31-5); [Dai et al.](#page-31-6) [\(2020\)](#page-31-6); [Bolton et al.](#page-31-7) [\(2021\)](#page-31-7). While this literature typically assumes exogenous security design for liquidity management, we characterize optimal liquidity risk management through an optimal long-term contract with a financier. We then implement this optimal contract via standard securities, such as credit lines, and distress resolution procedures, such as the US Bankruptcy Code, rationalizing their use to optimally manage liquidity in practice. Moreover, by endogenizing liquidity management contracts, we uncover a joint determination of liquidity management and financial constraints.

Our work also relates to the dynamic contracting literature that studies optimal risk-sharing between a principal and an agent under limited commitment, such as [Ai](#page-31-8) [and Li](#page-31-8) [\(2015\)](#page-31-8), [Ai et al.](#page-31-9) [\(2023\)](#page-31-9), and [Bolton et al.](#page-31-10) [\(2019\)](#page-31-10). Our model differs in that it highlights optimal financing from an intermediary in the presence of cash constraints and limited liability, resulting in defaultable debt as the optimal contract. [Rampini and](#page-32-5) [Viswanathan](#page-32-5) [\(2010\)](#page-32-5); [Rampini et al.](#page-32-6) [\(2014\)](#page-32-6) provide models in which limited enforcement constrains financing and creates a role for collateral. [Rampini and Viswanathan](#page-32-7) [\(2020\)](#page-32-7) applies their framework to distinguish between secured and unsecured debt. In these models, the optimal contract takes the form of state-contingent debt, which involves distress resolution without speaking to bankruptcy, liquidation, or changes in ownership. [Abel](#page-31-11) [\(2018\)](#page-31-11) develops a dynamic trade-off theory in which a (cash flow-based) borrowing constraint prevents shareholders from defaulting immediately. In contrast, in our model the borrowing constraint is optimally chosen to be either cash flow- or asset-based.

Our paper also relates to the extensive literature on corporate bankruptcy and its resolution.[1](#page-4-0) Related to our work, [Von Thadden et al.](#page-32-8) [\(2010\)](#page-32-8) derive optimal bankruptcy rules in light of incompatible promises to different creditors in an incomplete contracting framework. [Antill and Grenadier](#page-31-12) [\(2019\)](#page-31-12) present a model of bankruptcy choice between Chapter 7 and Chapter 11 that is based on dynamic bargaining. We contribute by showing how distress resolution akin to bankruptcy procedures arises as a feature within a complete long-term contract that facilitates optimal risk-sharing.

Finally, our paper also relates to the dynamic contracting literature that studies corporate settings with moral hazard but without liquidity management. [Bolton and](#page-31-13) [Scharfstein](#page-31-13) [\(1990\)](#page-31-13), and more recently, [DeMarzo and Sannikov](#page-31-14) [\(2006\)](#page-31-14); [Biais et al.](#page-31-15) [\(2007\)](#page-31-15); [DeMarzo and Fishman](#page-31-16) [\(2007\)](#page-31-16); [Sannikov](#page-32-9) [\(2008\)](#page-32-9); [DeMarzo et al.](#page-31-17) [\(2012\)](#page-31-17); [Malenko](#page-32-10) [\(2019\)](#page-32-10) show how financing constraints can arise endogenously as the result of a agency conflicts. Using techniques from this literature, we solve for the optimal contract between the firm's shareholders and the intermediary in the absence of agency conflicts but when the firm

1. [White](#page-32-11) [\(2017\)](#page-32-11) reviews this literature which typically takes debt as given or assumes incomplete contracts to derive debt.

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faces liquidity constraints and therefore must both manage its liquidity and design the contract, inducing endogenous financing capacity.

2. MODEL SETUP

Time $t \geq 0$ is continuous and infinite. We consider a firm whose assets produce cash flows X_t with stationary increments

$$
dX_t = \mu dt + \sigma dZ_t,\tag{1}
$$

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where dZ_t is the increment of a standard Brownian Motion. The firm is owned by risk-neutral investors who are hand-to-mouth, i.e., they consume all payouts and do not have any resources to inject into the firm. Access to external financing from newly arriving risk-neutral investors occurs only infrequently. An intermediary (distinct from the investors) is available to continuously provide (bridge) financing at a premium. Both the investors and the intermediary discount the future at the risk-free rate of $r > 0$. The intermediary and investors sign a long-term contract C at time $t = 0$. This contract, $C = (Div, I, \Delta M)$, stipulates cumulative payouts Div_t to investors, money raised from new investors upon access to external financing ΔM_t , and cumulative transfers I_t to and from the intermediary. Cash flows dX_t are publicly observable, verifiable, and contractible. As will become clear, within the optimal contract, the investors act as the firm's shareholders, who receive dividend payouts $dDiv_t$. In anticipation of this result, we refer to the investors as the shareholders and to the value of their stake as the firm's equity value. Further, external financing takes the form of equity injections, which we often refer to as refinancing. However, we emphasize that we do not impose ex-ante restrictions on the form of the contract.

As in [Hugonnier et al.](#page-32-1) [\(2015\)](#page-32-1), the firm can only access financing from competitive and risk-neutral investors at Poisson times with constant intensity $\pi \geq 0$. Here, $d\Pi_t = 1$ indicates access to external financing or market access at time t. We assume $d\Pi_0 = 1$ so that the initial shareholders (owners) can raise outside financing at inception by selling part of the firm. Once outside investors provide financing, they become hand-to-mouth and thus indistinguishable from the previous shareholders. This assumption reflects capital supply risk or proxies for frictions that cause a delay between the firm's need for financing and its access to broader markets.^{[2](#page-5-0)} The key implication of the outside investors becoming hand-to-mouth after providing capital is that dividend payouts to shareholders must be non-negative, i.e., $dDiv_t \geq 0$ at all times $t \geq 0$, including at refinancing times with $d\Pi_t = 1$.

The firm's financial constraints and possibility of negative cash flow shocks imply that the firm has an incentive to accumulate cash M_t via retained earnings. The cash balance held within the firm accrues interest at the rate $r - \lambda$ where r is the common interest rate and $\lambda \in (0,r)$ represents a carry cost of cash.^{[3](#page-5-1)} The dynamics of cash reserves M_t are

$$
dM_t = dX_t + (r - \lambda)M_t dt - dDiv_t - dI_t + \Delta M_t d\Pi_t.
$$
\n⁽²⁾

Absent access to equity financing, all cash flow realizations dX_t , payouts to shareholders $dDiv_t \geq 0$, and transfers to/from the intermediary $dI_t \geq 0$ flow through the cash balance

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^{2.} One may interpret the time it takes to arrange for financing as proxying for asymmetric information — outside investors take time to verify information. The intermediary as a specialist does not face such a delay.

^{3.} This assumption is standard (see, e.g., Décamps et al. [2011](#page-31-1) and [Bolton et al.](#page-31-0) [2011\)](#page-31-0) and prevents the firm from saving itself out of the constraint. Assuming impatient investors leads to similar results.

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 M_t . Unlike shareholders, the intermediary can provide financing to the firm at any time, so dI_t can be negative. However, this source of financing is costly, as we formalize below.

The cash balance of the firm at $t= 0^-$, i.e., before the contract is signed, is $M_{0^-} = 0$, and it must remain non-negative throughout, $M_t \geq 0$ for all $t \geq 0$. This constraint implies that if M_t reaches zero, the intermediary must either inject the necessary funds or the firm must liquidate or, equivalently, conduct a fire-sale of assets. Liquidation occurs at a stopping time $\tau \in [0,\infty]$, and $dDiv_t = dI_t = dX_t = 0$ for all $t > \tau$. At liquidation time τ , the firm realizes cash flows equal to the assets' liquidation value, i.e., $dX_{\tau} = L \in [0, \mu/r)$, so liquidation is costly compared to the first-best. Thus the total liquidation value of the firm is $L+M_{\tau}$.

2.1. Optimal Contracting Problem

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Given a contract \mathcal{C} , we can write the intermediary's certainty equivalent continuation value as

$$
Y_t = \mathbb{E}_t \left[\int_t^\tau e^{-r(s-t)} \left(dI_s - dK_s \right) \right]. \tag{3}
$$

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We refer to Y_t as the intermediary's promised payments, or as the intermediary's stake, because it represents a portion of firm value promised to the intermediary. In [\(3\)](#page-6-0), dK_t is the intermediary's endogenous cost of providing financing to the firm and is implicitly defined by the difference between the risk-neutral and the intermediary's valuation of the transfer process. We work with dK_t here because it saves on notation and it is equivalent to expressing Y_t using the intermediary's preferences over consumption directly. We will discuss dK_t further once we characterize the dynamics of Y_t . The intermediary has an outside option normalized to zero. It can always part from the contract and receive its outside option whenever it is privately optimal to do so and is thus subject to limited commitment, i.e., $Y_t \geq 0$ at any time $t \geq 0.4$ $t \geq 0.4$

We denote the firm's equity value, i.e., the shareholders' value function, by P_t . Upon access to new equity financing the firm raises ΔM_t dollars from competitive risk-neutral investors at fair value by issuing ΔM_t dollars worth of new equity. Refinancing changes total equity value from $P_{s^-} \equiv \lim_{s \uparrow t} P_s$ pre-refinancing to $P_t \equiv \lim_{s \downarrow t} P_s$ post-refinancing, while existing shareholders' are diluted and their post-refinancing payoff is $P_t-\Delta M_t$. The shareholders' inability to inject cash into the firm and financial frictions together imply the joint constraints

$$
dDiv_t \ge 0 \quad \text{and} \quad \Delta M_t \le P_t,\tag{4}
$$

as current shareholders cannot issue equity worth more than the total value of the firm post-refinancing P_t . We refer to [\(4\)](#page-6-2) as the shareholders' limited liability constraint. If the firm issues the maximal amount $\Delta M_t = P_t$, existing shareholders are completely diluted.

At time t, given a contract C , the equity value of the current shareholders is the expected discounted stream of future dividends less the costs of refinancing via dilution,

$$
P_t = \mathbb{E}_t \left[\int_t^\tau e^{-r(s-t)} (dDiv_s - \Delta M_s d\Pi_s) \right]. \tag{5}
$$

4. This constraint prevents the firm from raising a large amount of cash and saving it with the intermediary, avoiding the internal cost of cash. Qualitative results are unchanged if we assume $Y \ge Y$ for $\underline{Y} < 0$.

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From [\(4\)](#page-6-2) it immediately follows that $P_t \geq 0$. For all $t \geq 0$, the optimal contract maximizes

$$
P_{0-} = \max_{\mathcal{C}} \mathbb{E}\left[\int_{0-}^{\tau} e^{-rt} (dDiv_t - \Delta M_t d\Pi_t)\right] \text{ s.t. limited liability (4), } Y_t, M_t \ge 0,
$$
 (6)

where the intermediary's stake Y_t is given by [\(3\)](#page-6-0) with initial value $Y_{0-} = 0$, the cash balance M_t follows [\(2\)](#page-5-2) with initial balance M_0 = 0, and the equity value P_t is given by [\(5\)](#page-6-3). Table [A1](#page-20-0) provides an overview of variables used in the model while Table [1](#page-20-0) does so for parameters.

3. MODEL SOLUTION

We now solve the model and derive the optimal contract. We gain tractability by showing that the difference between the firm's cash holdings and the intermediary's future promised payments is a sufficient statistic for the state of the firm. All proofs and additional required derivations can be found in the [Online Appendix.](#page-0-0)

3.1. Intermediary Valuation

The following lemma gives the dynamics of total compensation to the intermediary, Y_t+I_t .

Lemma 1. For any contract \mathcal{C} , the intermediary's continuation payoff can be expressed as

$$
dY_t + dI_t = rY_t \cdot dt + dK_t + \beta_t \sigma dZ_t + \alpha_t (d\Pi_t - \pi dt),\tag{7}
$$

where β_t captures the intermediary's exposure to Brownian cash flow shocks dZ_t , while α_t captures the intermediary's exposure to the (compensated) market access process $(d\Pi_t-\pi dt)$.

We refer to equation [\(7\)](#page-7-0) as the *promise keeping* constraint. It pins down the sum of current transfers dI_t and changes in promised payments dY_t , but not the split between the two. Our assumptions on liquidation together with [\(7\)](#page-7-0) require that at the time of liquidation τ , the intermediary receives a lumpy payout of $dI_{\tau} = Y_{\tau-}$.

Intermediary cost of financing. We microfound dK_t in ?? by assuming the intermediary has CARA preferences with risk-aversion ρ and can privately saving/borrow at rate r. This yields dK_t as a function of α_t and β_t only:^{[5](#page-7-1)}

$$
\frac{dK_t}{dt} = k(\alpha_t, \beta_t) = \underbrace{\sigma^2 \cdot \left(\frac{\rho r \beta_t^2}{2}\right)}_{t} + \underbrace{\pi \cdot \left(\alpha_t - \frac{1 - e^{-\rho r \alpha_t}}{\rho r}\right)}_{t} \qquad (8)
$$

 $Risk-premium$ dZ_t exposure Risk-premium $(d\Pi_t - \pi dt)$ exposure

We interpret $1/\rho$ as the intermediary's limited risk-bearing capacity due to regulatory or capital constraints. Further, we assume this risk-bearing capacity is constant for

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^{5.} The cost function we specify in [\(8\)](#page-7-2) is without loss of generality given CARA preferences for the intermediary. Specifically, we can characterize any abtirary contract by the loadings α and β and transfer process dI. Given CARA preferences, the cost function dK_t must take the form in [\(8\)](#page-7-2). For preferences other than CARA, however, other state variables such as wealth might enter dK_t .

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two reasons: First, the intermediary, which may represent a group of bank or nonbank lenders investing in many firms, is large relative to the firm. Thus, while the intermediary requires some compensation for bearing firm risk, its risk-bearing capacity is not significantly affected by the performance of one individual firm. Second, this assumption lends tractability to our model; otherwise, one would have to track the additional state variables that drive the intermediary's risk-bearing capacity such as its net worth.[6](#page-8-0)

Autarky value. Consider the autarky value of the firm to the intermediary if it does not have access to outside financing and continues operations. The firm does not retain cash due to the firm's carry-cost-of-cash, and the intermediary fully absorbs all shocks for an autarky value of

$$
Y^A \equiv \frac{\mu}{r} - \frac{\rho}{2}\sigma^2,\tag{9}
$$

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which is the first-best value, μ/r , less a risk-adjustment term.^{[7](#page-8-1)} If $Y^A \lt L$, rather than operating the firm in autarky for a value Y^A , the intermediary instead immediately liquidates it for a value of L. The value Y^A will play a pivotal role in interpreting our later results.

3.2. Equity Valuation and the HJB Equation

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In principle, the dynamic optimization of the shareholders' value function depends on two state variables: the intermediary's promised payments Y_t , and the firm's cash holdings M_t . We heuristically show how to reduce the problem to a single state variable called net liquidity

$$
C_t \equiv M_t - Y_t. \tag{10}
$$

Observe that for any one-time transfer ΔI from the firm to the intermediary

$$
C_t = M_t - Y_t = (M_t - \Delta I) - (Y_t - \Delta I) \tag{11}
$$

by [\(7\)](#page-7-0). Thus, C_t is invariant to such transfers so we can freely adjust Y_t freely without affecting net liquidity, which in turn implies that Y_t is a control variable and C_t is the state variable. The dynamics of C are characterized in $\mathsf{?}\mathsf{?}$ by combining [\(2\)](#page-5-2) and [\(7\)](#page-7-0).

In what follows, we omit time subscripts unless necessary.

Limits to Deferred Payments. Even though Y is a control variable, it is constrained: First, the intermediary's limited commitment requires $Y \geq 0$. Second, the definition of net liquidity [\(10\)](#page-8-2) and the physical constraint on cash $M \geq 0$ together imply that $Y \geq -C$. Combining, we have

$$
Y \ge \max\{0, -C\}.\tag{12}
$$

Limits to Refinancing. Let C^* be the post-refinancing level of C . When the firm has access to new equity investors, it issues total claims worth ΔM to increase cash holdings from M to M^* and cover payouts to the intermediary dI. By [\(7\)](#page-7-0), at market access

^{6.} We could assume that equity investors are risk-averse, in that they apply a stochastic discount factor. As long as it is not optimal to sell the entire firm to the intermediary, the model's dynamics remain similar.

^{7.} Setting $dI_s = dX_s$ in [\(3\)](#page-6-0) and $\beta_s = 1$ and $\alpha_s = 0$ in [\(8\)](#page-7-2) delivers the result.

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times we have $\alpha = dI + dY = dI + (Y^* - Y)$, i.e., the change in total compensation to the intermediary upon refinancing α is equal to its immediate payouts dI plus any changes in promised payments $Y^* - Y$. At refinancing, the sources and uses of funds accounting identity is given by

$$
\underline{\Delta M} = \underline{M^* - M} + \underline{\alpha + Y - Y^*} = C^* - C + \alpha, \qquad (13)
$$
\nCapital Raised Cash Replenishment: Payouts to Intermediate

which implies that optimizing over $(\Delta M, \alpha)$ is equivalent to optimizing over (C^*, α) . Combining [\(13\)](#page-9-0) with the limited liability constraint [\(4\)](#page-6-2), we derive the following Lemma.

Lemma 2. Any contract respecting promise keeping (7) and limited liability (4) must satisfy

$$
\alpha \le [P(C^*) - C^*] + C. \tag{14}
$$

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Constraint [\(14\)](#page-9-1) is a key feature of the model that follows naturally from the assumption that shareholders cannot freely inject capital into the firm. This assumption contrasts with much of the prior literature that is often focused on impediments to the sharing of cash flow-risk, for example due to moral hazard or limited enforcement. In our context, such impediments would manifest as forces that shape β . Constraint [\(14\)](#page-9-1) instead highlights a restriction on a novel risk-sharing problem: $\alpha > 0$ means that existing equity holders and the intermediary share the risk of delays to market access. Limited liability and promise keeping, however, restrict how much of this risk shareholders can lay off to the intermediary. In our implementation of the optimal contract, this constraint implies a new role for bankruptcy.[8](#page-9-2)

HJB Equation. We conjecture and verify that equity value can be expressed as a function of net liquidity only, $P_t = P(C_t)$. To solve the shareholders' dynamic problem [\(6\)](#page-7-3), we solve for the optimal $P(C)$ for a given level of C. With $P(C)$ in hand, we then determine the payoff to the original shareholders (owners) by determining the initial choice of C_0 . We conjecture that the firm optimally makes dividend payouts to shareholders at an endogenous upper boundary $C = \overline{C}$, and that it either liquidates or receives sufficient financing to stay alive at some endogenous lower boundary C . Thus, in the continuation region $C \in (\underline{C}, \overline{C})$, given the dynamics of C derived from combining [\(2\)](#page-5-2) and [\(7\)](#page-7-0), we have the HJB

$$
r \cdot P(C) = \max_{\beta, Y} \left\{ P'(C) \left[\mu + (r - \lambda)C - \lambda Y - \sigma^2 \frac{\rho r}{2} \beta^2 \right] + P''(C) \frac{\sigma^2}{2} (1 - \beta)^2 \right\}
$$

$$
+ \pi \cdot \max_{C^*, \alpha} \left\{ P'(C) \left(\frac{1 - e^{-\rho r \alpha}}{\rho r} \right) + \left[(P(C^*) - C^*) - (P(C) - C) - \alpha \right] \right\}. \tag{15}
$$

subject to (12) and (14) . The term in square brackets on the second line is the change in existing shareholders value upon refinancing, $P(C^*) - P(C) - \Delta M$, after plugging in (13) . Note that the right-hand-side only depends on the state variable C and controls

^{8.} We investigate limits to the shareholders' ability to commit in Section [7.1](#page-26-0) by using the generalized constraint $\alpha \leq [P(C^*)-C^*]-[(1-\nu)P(C)-C], \nu \in [0,1]$, where ν measures the strength of commitment.

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 (α, β, Y, C^*) with constraints that only depend on C and the controls themselves. As the boundary conditions below also only depend on the value of C at the boundaries, we can express equity value as a function of C alone, $P_t = P(C_t)$.

Payout boundary. The payout boundary satisfies smooth pasting and super contact conditions,

$$
P'(\overline{C}) = 1 \text{ and } P''(\overline{C}) = 0. \tag{16}
$$

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For now, we assume that a well-behaved, non-negative, and twice continuously differentiable solution to [\(15\)](#page-9-3) exists on the endogenous state space (C,\overline{C}) subject to (12) , (14) , and (16) for any given C. In Online Appendix A.12, we establish existence and uniqueness of such a solution. Proposition [1](#page-10-1) summarizes our findings.

Proposition 1. Equity value under the optimal contract can be expressed as function of C only, $P_t = P(C_t)$, and solves the HJB [\(15\)](#page-9-3) on the endogenous state space $(\underline{C}, \overline{C})$ subject to [\(12\)](#page-8-3), [\(14\)](#page-9-1), and [\(16\)](#page-10-0). Equity value is strictly concave on $(\underline{C}, \overline{C})$, so that $P''(C) < 0$ and $P'(C) > 1$ for $C < \overline{C}$. Optimal dividend payouts dDiv cause C to reflect at \overline{C} and are zero in the interior of the state space. The payout boundary is strictly positive, $\overline{C} > 0$.

The concavity of equity value implies that shareholders are effectively risk-averse, since liquidation is inefficient, access to external equity financing limited, and intermediary funds costly. To withstand cash flow shocks absent access to equity financing, the firm accumulates cash and delays payouts until C reaches the payout boundary.

3.3. Optimal Controls & Lower Boundary

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Optimal Controls. First, the FOC of the HJB with respect to C^* yields $P'(C^*(C))=1$ and without loss of generality 9

$$
C^* = C^*(C) = \overline{C}.\tag{17}
$$

The original shareholders' payoff $P(C_0) - C_0$ is maximized via initial equity issuance at $C_0 = \overline{C}$.

Second, due to the carry cost of cash λ , the contract picks the lowest Y possible subject to (12) :

$$
Y(C) = \max\{-C, 0\}
$$
 and $M(C) = \max\{C, 0\}.$ (18)

Given the strictly positive payout boundary $\overline{C} > 0$, we can now write the transfer process as

$$
dI = \mu_I(C)dt + \sigma_I(C)dZ + \alpha_I(C)d\Pi \quad \text{with} \quad \alpha_I(C) \equiv \alpha(C) + Y(C). \tag{19}
$$

Rewriting [\(14\)](#page-9-1), we see that the payout to the intermediary upon market access is bounded by Total Resale Value

Total Resale Value
\n
$$
\underbrace{\alpha(C) + Y(C)}_{\text{Payouts to Intermediary}} \leq \underbrace{\overbrace{P(\overline{C}) - \overline{C}}_{\text{Post-refi Net Value}} + \underbrace{M(C)}_{\text{Pre-refi Cash}}.
$$
\n(20)

Third, setting $\beta > 0$ transfers cash flow risk to the intermediary, reducing the volatility of C at the cost of a flow risk-premium of $\sigma^2 \frac{\rho r}{2} \beta^2$ in [\(7\)](#page-7-0). The FOC with respect to β

9. Any $C^* > \overline{C}$ also fulfills the FOC but leads to an immediate dividend of $C^* - \overline{C} > 0$ upon refinancing.

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yields

$$
\beta(C) = \frac{P''(C)}{P''(C) - \rho r P'(C)} \in [0,1].
$$
\n(21)

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Fourth, setting $\alpha > 0$ shifts payouts to the intermediary from financially constrained states to financially unconstrained states of the firm, at the cost of a flow risk-premium of $\pi \cdot \left(\alpha - \frac{1-e^{-\rho r \alpha}}{\rho r}\right)$ in [\(7\)](#page-7-0). The FOC with respect to α when [\(14\)](#page-9-1) is not binding yields

$$
\alpha = \alpha_U(C) \equiv \frac{\ln P'(C)}{\rho r}.
$$
\n(22)

Given that [\(14\)](#page-9-1) may be binding, the optimal $\alpha = \alpha(C)$ is characterized by

$$
\alpha(C) = \min\left\{\alpha_U(C), P(\overline{C}) - \overline{C} + C\right\} \ge 0.^{10}
$$
\n(23)

Optimal Lower Boundary. We now argue there exist an endogenous lower boundary C such that $C_t \geq C$ at all times t. For C to be a lower bound for C, it must be that either (i) the firm liquidates at C , or that (ii) C is either inaccessible or absorbing (absent refinancing), in which case we denote the lower boundary by C^S and the firm is not liquidated at $C = C^S$.

For (i), given that liquidation is inefficient, the firm delays liquidation as long as possible to the lowest boundary consistent with promise keeping $C = -L$. The key to (ii) is that for C to be a lower bound of C in the absence of liquidation, something we term continuation, it must not be crossed. This requires that as net liquidity C approaches C its volatility must vanish, requiring $\lim_{C \downarrow C} \beta(C) = 1$, while its drift and the shareholders' value function $P(C)$ both must stay non-negative. Intuitively, at C the intermediary keeps the firm alive by providing continuous financing and absorbing all cash flow risks. Further, it is optimal to delay setting $\beta = 1$ as long as possible due to the intermediary's cost of bearing risk, so that C^{S} is the lowest of all potential continuation boundaries, pinned down by $P(C^S)=0$, which requires the drift to vanish.

The following Lemma states the lower boundary in closed form as a function of \overline{C} :

Lemma 3. The lower boundary and the associated value of equity are given by

$$
\underline{C} = \min\left\{C^S, -L\right\} \quad with \quad P(\underline{C}) = 0. \tag{24}
$$

For $w(\cdot)$ representing the Lambert-W function, C^S is given by

$$
C^{S} = \frac{1}{\rho r} \left[w \left(\frac{\pi}{r} \exp \left\{ \rho r \left[\frac{\lambda}{r} \overline{C} + \frac{\pi}{\rho r^{2}} - \frac{\rho}{2} \sigma^{2} \right] \right\} \right) - \frac{\pi}{r} \right] - Y^{A} \in \left[-\frac{\mu}{r}, -Y^{A} \right].
$$
 (25)

At the lower boundary \underline{C} , the intermediary owns the entire firm and values it at $Y(\underline{C})=$ $-C$. To gain intuition about C^S , consider an approximation to [\(25\)](#page-11-1) by ignoring the

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^{10.} As we show in Lemma [3](#page-11-2) below, the lower boundary satisfies $C \ge -[P(\overline{C})-\overline{C}]$, which implies $\alpha(C) \geq 0.$

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required risk premium for α in [\(8\)](#page-7-2), i.e., $k(\alpha, \beta) \approx \sigma^2 \frac{\rho r}{2} \beta^2$. Then

$$
Y(C^{S}) = -C^{S} \approx \frac{r}{r+\pi} \underbrace{Y^{A}}_{\text{Autarky Value}} + \frac{\pi}{r+\pi} \underbrace{[P(\overline{C})-\overline{C}]}_{\text{Resale Value}}.
$$
 (26)

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The intermediary's valuation of the entire firm $Y(C^S)$ at the continuation boundary is approximately the weighted average of its (exogenous) autarky valuation Y^A and the (endogenous) gain from selling the firm to outside investors at the fair price $P(\overline{C})-\overline{C}$ upon the next equity market access as cash-holdings are zero, i.e., $M(C^S) = 0$.

The following Lemma will be useful in our implementation.

Lemma 4. When $\underline{C} = C^S$, the lower boundary is inaccessible.

Lastly, the following Lemma shows that the limited liability constraint [\(14\)](#page-9-1) always binds on the lower end of $\overline{[C,\overline{C}]}$ when $\overline{C} = C^S$, in which case the firm is never liquidated and the boundary is inaccessible. In this case, there exists a region in which the proceeds from raising equity are insufficient to implement the desired capital supply risk sharing $\alpha_U(C)$.

Lemma 5. When $\underline{C} = C^S$, constraint [\(14\)](#page-9-1) always binds in a neighborhood of \underline{C} .

3.4. Optimal Contract

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We now characterize the optimal financing arrangement by summarizing our previous results.

Proposition 2. Under the optimal contract, $P(\underline{C})=0$ where \underline{C} is given by [\(24\)](#page-11-3). Optimal controls (C^*, Y, β, α) are characterized by [\(17\)](#page-10-3)-[\(18\)](#page-10-4) and [\(21\)](#page-11-4)-[\(23\)](#page-11-5). If $\underline{C} = -L$, the firm liquidates once C reaches the lower boundary C and $\beta(C)$ < 1 for all $C \geq C$. If $\underline{C} = C^S$, the firm never liquidates and $\beta(\underline{C}) = 1$ while $\beta(C) < 1$ for all $C > \underline{C}$. The firm's initial liquidity choice coincides with the payout boundary, $C_0 = \overline{C}$.

Section [4](#page-14-0) shows a natural implementation of the optimal contract via defaultable debt subject to common bankruptcy procedures. Section [5](#page-20-1) presents numerical evaluations of the optimal contract with accompanying figures.

Asset- and Cash Flow-Based Financing Capacity. In the optimal contract, the intermediary provides financing against promised payments, as long as the value of these promises Y does not exceed the firm's financing capacity defined as

$$
\overline{Y} \equiv Y(\underline{C}) = -\underline{C} = \max\{L, -C^S\}.
$$
\n(27)

When $C = -L$, financing capacity is *asset-based* and is determined by the liquidation value assets. When $C < 0$, the firm taps into intermediary financing against future promised payments $Y(C) > 0$ and pledges the firm's assets to the intermediary so as maintain promise keeping. Upon liquidation at $C = -L$, the intermediary seizes the entire liquidation value to receive its promised payoff $Y(\underline{C})=L$.

When $\underline{C} = C^S$, financing capacity is *cash flow-based*, and the intermediary provides sufficient financing to prevent liquidation, for which it is compensated via future promised

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payments. The intermediary effectively obtains a stake in the firm which backs future promised payments. Since the contract cannot allocate a stake in the firm greater than full ownership, the intermediary's valuation of the firm, including the value of future refinancing opportunities, constrains the amount of financing that the intermediary provides against promised payments. Intuitively, for the firm to be able to obtain financing against future cash flows, the firm must not be liquidated beforehand so that these cash flows indeed realize.

A key insight from the model is that a firm's financing capacity C depends on intermediary and market characteristics in addition to firm characteristics.

Corollary 1. When ρ is sufficiently large or $Y^A < L$ and π is sufficiently small, then $\underline{C} = -L$, while for ρ sufficient small or π sufficiently large, $\underline{C} = C^S$.

First, consider $\rho \rightarrow \infty$, so the intermediary has zero risk-bearing capacity, leading to $\beta(C) = \alpha(C) = 0$ and $C = -L$ by [\(21\)](#page-11-4), [\(23\)](#page-11-5), and [\(24\)](#page-11-3). The intermediary is still willing to provide financing against promised payments. Thus, although the intermediary covers all cash flow shocks when $C < 0$, it cannot bear cash-flow risk. By [\(7\)](#page-7-0), $dI + dY = rY dt$, so future promised payments grow at the risk-free interest rate r and are fully backed by the assets' liquidation value L . In this case, financing capacity is asset-based.

Second, consider $\pi = 0$, so there is no further equity market access. From [\(25\)](#page-11-1), we have $C^{S} = -Y^{A}$, and the intermediary's going concern value of the firm is exogenously pinned down by the intermediary's risk-bearing capacity $1/\rho$ and the parameters of the cash-flow process as derived in (9) . In other words, at $C = \underline{C}$, the intermediary holds the entire firm. However, since it can never resell the firm, the shape of the future contract does not affect its current going-concern valuation for the firm. Thus, the shape of the future contract only matters when $\pi > 0$ and operates through future resale value, which in turn endogenously affects the intermediary's current going-concern valuation, in that $-C^{S} > Y^{A}$. Further, when $Y^{A} < L < -C^{S}$, financing capacity is cash-flow based, but absent equity market access it would be asset-based.

3.5. Discussion of the Mechanism (1)

The key force that drives this model's optimal contract and the firm's endogenous financing capacity, i.e., the maximal promised payments Y , is the interplay of the risksharing of cash-flow risk β with the novel risk-sharing of capital supply risk α . To illustrate this mechanism, let us examine the optimal contract when we incrementally add the ability of the firm and the intermediary to share cash flow risk and capital supply risk.[11](#page-13-0)

First, suppose the firm and the intermediary are unable to share any risks, $\alpha = \beta =$ 0. The firm can still use transfers and promise payments so that $Y \geq 0$. However, the contract cannot expose the intermediary to any risk, so just as in the case of $\rho \rightarrow \infty$ we discussed above, $\alpha = \beta = 0$ implies $C = -L$, and there is no scope for cash flow-based financing. The model then reduces to a simple cash-holding problem as in [Hugonnier](#page-32-1) [et al.](#page-32-1) [\(2015\)](#page-32-1) with the addition of risk-free borrowing up to the firm's exogenous financing capacity of L.

Next, suppose the firm and the intermediary can share capital supply risk, but not cash-flow risk, $\beta = 0$. The firm now must liquidate at $\underline{C}_{\beta=0} = -L$ just as if the firm cannot

11. We separately discuss the mechanism in relation to the implementation in Section [4.2.](#page-17-0)

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share any risk with the intermediary, albeit for a more subtle reason. When $\beta = 0$, the intermediary cannot own the firm and all promise payments to the intermediary must be satisfied by transfers dI. Moreover, the contract cannot influence the volatility of C_t , so that if $C_t < L$, there are paths for the firm that lead to promised payouts Y that would exceed the risk-neutral present value of the firm μ/r , a clear violation of promise keeping.

Finally, suppose the firm and the intermediary can share cash flow risk but not capital supply risk, $\alpha = 0$. This effectively implies that the intermediary cannot benefit from the gains of equity issuance.^{[12](#page-14-1)} As a consequence, the intermediary's valuation of the firm does not reflect the gains from reselling the firm to new equity investors. That is, the lower boundary associated with continuation is consequently equal to the intermediary's autarky value $C_{\alpha=0}^{S} = -Y^{A}$. In other words, the firm's financing capacity does not depend on the intensity of capital market access. While there is scope for cash flow-based financing, the determination of the financing constraint is essentially exogenous.

4. IMPLEMENTING THE CONTRACT

We implement the optimal contract with a debt claim held by the intermediary. Up to this point, the state variable of the contract is the net liquidity $C = M - Y$ of the firm, which contains the forward looking promise Y to the intermediary. While this is a natural variable for shareholders to consider when deciding on payout and financing policies, standard securities typically do not explicitly specify payouts contingent on future payout promises. We show that we can implement the optimal contract based on the past transfer process dI_t .

4.1. Credit Line, Control Rights, and Bankruptcy

Financial Overhang. Refinancing from C to \overline{C} changes total equity value by an amount $P(\overline{C})-P(C)$ but by [\(13\)](#page-9-0) and [\(14\)](#page-9-1) changes existing shareholders' value by an amount

$$
J(C) \equiv P(\overline{C}) - \Delta M - P(C) = [P(\overline{C}) - \overline{C}] - [P(C) - C] - \alpha \ge -P(C). \tag{28}
$$

Figure [1](#page-15-0) depicts the optimal $J(C)$ by a solid red line and the negative of the shareholder's value function $P(C)$ by a dotted black line. In particular, for $J(C) < 0$ equity holders lose value through dilution when raising new equity. Intuitively, the firm faces a *financial* overhang problem when it raises new equity in such states: raising equity financing is only possible if shareholders agree to take a loss from dilution. In practice, it may prove difficult for shareholders to directly commit to take such a loss. Thus, in the absence of direct commitment, the contract must allocate control rights to the intermediary for all states C with $J(C) < 0$ to implement refinancing in those states.

Accounting for Past Transfers. For any time $t>0$, define the last refinancing time $\tau^{\Pi}(t) \equiv \sup\{s \le t : d\Pi_s = 1\}$. Let T_t be the cumulative net transfers received from the intermediary since the last refinancing time, i.e., over $s \in (\tau^{\Pi}(t), t)$, with each transfer dI_s compounding at some endogenous rate. We now characterize T_t as a function of C_t :

12. Note $\alpha = 0$ implies by [\(19\)](#page-10-5) that even though Y is fully paid out upon market access due to promise keeping, no other payments to the intermediary occur.

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Figure 1 Bankruptcy and Control Rights. Schematic graph of the different regions of the value of refinancing to existing shareholders under optimal (Y, β, α) .

Proposition 3. For dI defined by the optimal (Y, α, β) given in [\(18\)](#page-10-4), [\(21\)](#page-11-4), and [\(23\)](#page-11-5), let

$$
T_t := -\int_{\tau}^t \int_{t}^t \hat{r}_u du \, dI_s. \tag{29}
$$

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If $T_t = T(C_t)$ is Markov, then the pair $(T(C), \hat{r}(C))$ is unique, $T'(C) < 0$,

$$
T(C) = \alpha_U(C) + Y(C) \quad and \quad \hat{r}(C)T(C) = \frac{\lambda}{\rho r} 1_{\{C \ge 0\}} + rY(C). \tag{30}
$$

With Proposition [3](#page-14-2) in hand, we can change the state variable from forward looking C_t to backward looking $T_t = T(C_t)$.

Defaultable debt as the optimal contract. The proof of Proposition [3](#page-14-2) establishes that any Markovian contract with respect to C featuring optimal cash flow risk-sharing β and promises Y can be summarized by a unique $T(C)$, and that this quantity is linked to the unconstrained optimal choice of α , $\alpha_U(C)$. Note from [\(19\)](#page-10-5) that the choice of α determines the payout in the event of refinancing. By [\(20\)](#page-10-6), the optimal repayment to the intermediary upon refinancing equals min $\{T(C), P(\overline{C})-\overline{C}+M(C)\}\)$, i.e., the minimum of $T(C)$ and the total resale value of the firm to new equity investors upon capital market access. As such, the repayment resembles that of defaultable debt with balance (facevalue) $T(C)$, and we will often refer to the intermediary as the *creditors*. Lemma [5](#page-12-0) shows that (14) binds in some neighbourhood of C under cash flow-based financing. In this case, some repayment shortfall occurs in optimum as a risk-sharing tool. Further, this interpretation identifies financial overhang as a form of debt overhang. Consequently, the optimal contract does not fully avoid debt overhang, necessitating the allocation of control rights to the creditors.

Bankruptcy and control rights. We achieve this control right allocation via bankruptcy or threat thereof from debt covenant violations. Specifically, we need to structure the covenant so that it is violated whenever $J(C) < 0$. It can be a balance sheet covenant, e.g., a maximum debt-to-asset ratio, or a financial covenant, e.g., an

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earnings-based covenant which is violated after a sufficient string of negative cash flow realizations. Figure [1](#page-15-0) illustrates.

For high C such that $J(C) > 0$ we are in the Voluntary Refinancing region. Shareholders voluntarily refinance because they gain from doing so, and creditors are repaid in full.

For low C such that $J(C) < 0$, three cases arise. First, in the Forced Refinancing region, $J(C) \in (-P(C),0)$ so that the covenant is violated and existing shareholders face the threat of bankruptcy. However, in these states refinancing proceeds are sufficient to repay the creditors in full while not fully wiping out all equity. Thus, rather than facing bankruptcy and losing all continuation value, shareholders voluntarily pay off the creditors upon finding new equity financing, in the process preserving some value for themselves.

In contrast, in the Chapter 11 region constraint [\(14\)](#page-9-1) binds and $J(C)=-P(C)$. Recall that this implies the refinancing proceeds are insufficient to fully pay back the creditors, so shareholders have no incentive to refinance on their own. Consequently the creditors enforce the covenant and force the firm into Chapter 11 bankruptcy. If the opportunity to raise new equity arrives in this region, the existing shareholders are fully wiped out.

Finally, in the Chapter 7 region the firm runs out of cash as the credit line is exhausted, and consequently the firm is liquidated. As Chapter 7 can only be reached from Chapter 11, this implies that the bankruptcy is converted from Chapter 11 to Chapter 7. Lemma [4](#page-12-1) established that Chapter 7 can only be reached under asset-based financing, i.e., $C = -L$.

Credit line repayment and bankruptcy resolution. Given the preceding discussion, there are four cases to credit line repayment. First, credit lines are gradually repaid after positive cash flow realizations. Second, when the firm's liquidity reserves are sufficiently high, i.e., in the Voluntary Refinancing and Forced Refinancing regions in Figure [1,](#page-15-0) credit lines are repaid in full. Third, when the firm is in distress in the Chapter 11 region, i.e., for low C such that (14) is binding, its creditors force it to enter Chapter 11 bankruptcy and the firm continues operations. If the firm finds new equity investors, the creditors take a partial write-down while the existing equity claims are wiped out. The firm then emerges from bankruptcy under the new ownership, completing the reorganization. The firm may also emerge from bankruptcy following a string of positive cash flow realizations without new equity infusions. Fourth, while in bankruptcy, the firm may hit its financing capacity at Chapter 7 in Figure [1,](#page-15-0) i.e., for $C = C$, in which case it is liquidated, akin to converting Chapter 11 to Chapter 7. In all cases, repayments respect the absolute priority rule $(APR).$ ^{[13](#page-16-0)}

Modes of Financing and Bankruptcy Codes. As Lemma [4](#page-12-1) established, Chapter 7 is never reached in the cash-flow based financing case, i.e., $\underline{C} = C^S$. Thus it follows that cash flow-based financing is associated with only Chapter 11 reorganization, while asset-based financing, i.e., $C = -L$, is associated with both Chapter 11 reorganization and Chapter 7 liquidation. Different from bargaining-based models of bankruptcy, such as [Antill and Grenadier](#page-31-12) [\(2019\)](#page-31-12), the current shareholders have full commitment power vis-a-vis the intermediary. Thus, different bankruptcy resolutions are not a consequence of bargaining, but endogenously arise from the shareholders' commitment to the optimal contract.[14](#page-16-1) Lastly, bankruptcy and its resolution are ex-ante efficient.

^{13.} The reason is that the states in which there is partial default on the credit line are exactly the

states in which [\(14\)](#page-9-1) is binding, implying existing equity holders are wiped out while the firm survives. 14. We investigate possible limits to this ability to commit, in the form of violations of APR, in Section [7.1.](#page-26-0)

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Instantaneous controls and long-term financing. One key observation is that even though (α, β, Y) are instantaneous controls in [\(15\)](#page-9-3), the optimal contract — via Proposition [3](#page-14-2) — allows a long-term financing interpretation. For example, α_t can be seen as instantaneous risk-sharing at time t of the realization of $d\Pi_t$ that trades off receiving a sure cash inflow of $\pi \left(\frac{1-e^{-\rho r \alpha_t}}{\rho r} \right) dt$ (essentially receiving cash in financially constrained states) against a lumpy cash outflow of $\alpha_t d\Pi_t$ that occurs with probability πdt (essentially delivering cash in financially unconstrained states). Importantly, α being a choice variable it has no persistence per se, so the current choice of α need not reflect the path of α . For arbitrary $\beta(C)$, a Markovian $T(C)$ can still be derived, but it has no apparent connection to $\alpha(C)$. However, by the continuity of the optimization in the HJB and the underlying state variable C , [\(30\)](#page-15-1) implies that the sequence of optimal (Y_s, α_s, β_s) 's along any path looks like long-term financing with repayment $\alpha_t + Y_t$ linked to the total money drawn down T_t .

4.2. Discussion of Mechanism (2)

The implementation highlights a key role played by risk-sharing over supply uncertainty. As discussed in Section [3.5,](#page-13-1) it is the interplay of risk-sharing of both cash-flow risk β and capital supply risk α that makes the choice between asset- and cash flow-based financing endogenous. The implementation delivers the next part of our contribution: dynamic risk-sharing with an intermediary optimally takes the form of a debt contract that features common bankruptcy procedures for risk-sharing. Thus, it demonstrates that debt default in bankruptcy plays a distinct role from liquidation; default in bankruptcy implements optimal risk sharing, while liquidation eliminates future cash-flow risk.

To show why specifically risk-sharing over capital supply risk is needed for this result, let us again consider $\alpha = 0$. By [\(28\)](#page-14-3), we have $J_{\alpha=0}(C) > 0$ everywhere and therefore do not require state-dependent control rights. Thus, while existing shareholders gain upon refinancing, creditors always take a loss equal to $\alpha_U(C)$ regardless of the level of C. Recall from Section [3.5](#page-13-1) that $\alpha = 0$ implied that the risk-free debt capacity was pinned down by the intermediary's autarky value of the firm Y^A regardless of π . In this case, the firm could still issue risky debt, but doing so does not improve risk-free debt capacity. Imposing $\alpha = 0$ makes debt equally risky across the range of C while keeping risk-free debt capacity at Y^A . The optimal $\alpha(C)$ makes debt maximally risky when the firm is in distress (low C states) and safe otherwise (high C states), and thus expands riskfree debt capacity beyond Y^A . It also implies that APR must hold. Thus, α and the restriction [\(14\)](#page-9-1) are the key elements that link risk-free debt capacity to bankruptcy and its resolution.

How is the optimal bankruptcy process different from the firm transferring full ownership to the intermediary the first time [\(14\)](#page-9-1) binds, i.e., when the firm enters the Chapter 11 region in Figure [1?](#page-15-0) While in this region, the cash-flows to the intermediary are the same in either scenario, as the intermediary completely absorbs all cash flows and upon refinancing the intermediary has full ownership of the firm.^{[15](#page-17-1)} Thus, the difference has to arise from cash-flow outside the Chapter 11 region. Under the optimal contract, shareholders retain a stake in the firm even in the Chapter 11 region. This stake is valuable because the firm may emerge from bankruptcy through a sequence of positive cash

15. This is implied for the optimal contract by the fact that existing shareholders are completely wiped out.

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flows. Moreover, this value allows the the intermediary and the existing equity holders to optimally share cash flow risk even though the equity holders do not receive any cash flows unless the firm earns itself out of bankrupcty. Thus, an immediate ownership transfer is sub-optimal and the bankruptcy process optimally delays the ownership transfer to the intermediary for as long as possible.

4.3. Senior-secured and Unsecured Debt

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In the following, we refine the implementation of the optimal contract from Section [4.1](#page-14-4) by further splitting the balance $T(C)$ in [\(30\)](#page-15-1) into two separate and realistic debt securities, senior-secured debt and an unsecured credit line. This split is such that each of the securities implements specific functions of the optimal contract.

Senior-secured debt can take the form of short-maturity term debt or a credit line. It implements financing against promises, as captured by $Y(C)$; the balance of seniorsecured debt coincides with the intermediary's promised payments and is always repaid in full. The unsecured credit line has balance $\alpha_U(C)=T(C)-Y(C)$. It implements contracted risk-sharing $\alpha(C)$ and $\beta(C)$ and thus is risky.

Corollary 2. The optimal contract can be implemented via two securities that respect $APR: (1)$ Senior-secured debt with balance $Y(C)$, and (2) an unsecured, risky credit line with balance $\alpha_U(C)$ for $C \in (\underline{C}, \overline{C})$. At the dividend payout boundary, these balances are $Y(\overline{C})=\alpha_U(\overline{C})=0.$ For $C \in (\underline{C},\overline{C})$, the following holds:

1. Outstanding senior-secured debt $Y(C)$ grows with interest at rate r and rises and falls with transfers $dI^{Y}(C)$. Upon refinancing or liquidation, secured debt is repaid in full:

$$
dY(C) = rY(C)dt - dIY(C)
$$
\n
$$
dIY(C) = \left\{ \left[\mu - \sigma^2 \frac{\rho r}{2} \beta(C)^2 + \pi \frac{1 - e^{-\rho r \alpha(C)}}{\rho r} \right] dt + \sigma (1 - \beta(C)) dZ + Y(C) d\Pi \right\} 1_{\{C \le 0\}}.
$$
\n(31)

2. The balance of the unsecured credit line $\alpha_U(C)$ increases with a maintenance fee $\frac{\lambda}{\rho r}\mathbb{1}_{\{C\geq 0\}}$, and rises and falls with transfers $dI^{\alpha_U}(C)$:

$$
d\alpha_U(C) = \frac{\lambda}{\rho r} \mathbb{1}_{\{C \ge 0\}} dt - dI^{\alpha_U}(C) - [\alpha_U(C) - \alpha(C)]d\Pi
$$
\n
$$
dI^{\alpha_U}(C) = \left[\sigma^2 \frac{\rho r}{2} \beta(C)^2 - \pi \frac{1 - e^{-\rho r \alpha(C)}}{\rho r}\right] dt + \sigma \beta(C) dZ + \alpha(C) d\Pi.
$$
\n(32)

Upon refinancing, if [\(14\)](#page-9-1) is binding, the firm defaults on $[\alpha_U(C)-\alpha(C)]>0$ of the unsecured credit line, otherwise the unsecured credit line is repaid in full. Upon liquidation, the unsecured credit line is fully defaulted on.

Creditors have control rights over the firm for all C such that $J(C) \leq 0$ via debt covenants.

Senior-Secured Debt. The purpose of the senior-secured debt is to implement financing against future promised payment, as characterized by $Y(C)$. For brevity, in

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the following we refer to senior-secured debt simply as secured debt. This debt can take the form of short-maturity term debt, which matures instantaneously as in [Abel](#page-31-11) [\(2018\)](#page-31-11), or a credit line. Crucially, outstanding secured debt $Y(C)$ is always repaid in full. In our setting with constant firm fundamentals and continuous, stationary cash flows, secured debt does not provide any risk-sharing services. As such, it has an interest rate equal to the risk-free rate r . The firm relies on secured debt only when out of cash, i.e., it is a financing instrument of last resort. In other words, cash and secured debt are substitutes in our setting, in that they are not used simultaneously.

The firm's secured debt capacity, i.e., the maximum amount of secured debt available, equals \overline{Y} =−C and thus coincides with the firm's financing capacity in [\(27\)](#page-12-2). Therefore, secured debt capacity is either asset-based, i.e., determined by the liquidation of the firm's assets in that $\overline{Y} = L$, or cash flow-based, i.e., determined the firm's going concern value in that $\overline{Y} = -C^S$. Since the secured debt capacity matches the intermediary's valuation of the firm, it is natural to see senior debt as backed by the firm as collateral. The key function of the collateralized nature of secured debt is to implement the appropriate seniority structure.

Unsecured Credit Line. The firm's unsecured, risky credit line implements risksharing, that is, α and β . Repayments and drawdowns on the unsecured credit line in response to cash flow shocks are proportional to $\beta(C)$: Upon a negative cash flow shock of \$1, the firm draws down the credit line by $\mathcal{B}(C)$. Similarly, as can be seen from [\(32\)](#page-18-0), the speed with which the intermediary draws on the credit line, that is, $-dI^{\alpha}U(C)$, increases with $\alpha(C)$, while the balance of the credit line is paid back by the amount $\alpha(C)$ (including possible default) upon refinancing $d\Pi = 1$. Thus, the higher $\alpha(C)$, the larger the transfer from the intermediary to the firm. Again, from the discussion following Corollary [1,](#page-13-2) as the risk-bearing capacity of the intermediary vanishes, i.e., $\rho \rightarrow \infty$, there is no more risk-sharing and risky lending disappears, i.e., $\lim_{\rho\to\infty} \alpha_U(C)=0$.

Risk-sharing through the unsecured credit line occurs through lowered repayments in distress situations. First, there is default on the unsecured credit line when the firm raises new equity financing in distress when $\alpha(C) < \alpha_U(C)$, corresponding to bankruptcy. Second, the credit line features a preferential interest rate and a state-dependent maintenance fee, which is waived for $C < 0$. In our setting, due to our focus on a Markovian credit line implementation, this preferential interest rate equals zero, as it generates the optimal state-dependent repayments.

The interest rate of zero also reflects the lack of other frictions. For example, in Section [7.1,](#page-26-0) we show that in the absence of full commitment, the unsecured credit line carries an interest rate that is related to the expected loss from default.

The complementarity between secured and unsecured debt. Secured and unsecured debt in our implementation exhibit a form of complementarity, in that usage of one debt instrument facilitates usage of the other one. First, the use of the unsecured credit line as a liquidity risk management tool enhances risk-sharing and therefore increases the collateral value of the firm, thereby expanding the firm's secured debt capacity and potentially making it cash flow-based. Second, the unsecured credit line, which implements risk-sharing α and β , is necessary to prevent liquidation at C via $\beta(C)=1$ and thus for the secured credit line to have capacity beyond L, i.e., for financing capacity to be cash flow-based. Intuitively, unsecured debt allows the firm to offload risk to prevent liquidation, ensuring repayment of secured debt when it exceeds the liquidation value of assets. In distress, the unsecured credit line must take a loss and

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Definitions and Baseline Parameter Values for all Figures. The implied first-best value of the firm is $\frac{\mu}{r} = 3$ and the autarky value to intermediary is $Y^A = \frac{\mu}{r} - \frac{\sigma^2}{2} = 0$.

buffer negative cash flow shocks to facilitate the continuation of the firm, i.e., distress resolution without liquidation akin to Chapter 11 reorganization.

The complementarity between debt and equity. As stated in Corralary [1,](#page-13-2) higher π leads to can lead to a larger secured debt capacity by allowing the firm to raise new equity capital more frequently. An immediate consequence is that the better access to equity financing, the more likely the firm's financing capacity is cash flow-based rather than asset-based. On one hand, when the firm raises new equity financing, it repays the intermediary; that is, equity financing substitutes for debt financing. On the other hand, the prospect of future access to equity financing improves secured debt capacity by ensuring that secured debt is repaid. Thus, our results imply that secured debt and equity financing are static substitutes but dynamic complements.

An overlapping pecking-order. When the firm has cash reserves, it finances negative cash flow shocks with internal cash and unsecured debt. When the firm has run out of cash, it finances such shocks with unsecured and secured debt. That is, the firm uses unsecured debt financing in all states, while it resorts to secured debt financing only when out of cash. This is consistent with the practice of debtor-in-possession financing where secured loans allow the firm to continue operations in Chapter 11 bankruptcy.^{[16](#page-20-2)}

One might expect the opposite, that is, the firm first uses its available collateral to pledge for secured debt financing and, once collateral is exhausted, the firm raises unsecured debt financing. This intuition does not apply in our context because secured and unsecured credit line debt serve different functions. Unsecured debt is used to share liquidity risk with the intermediary. Such risk sharing is valuable, even when the firm has cash. Put differently, cash or secured debt and the unsecured credit line are complementary liquidity management tools. Secured debt is a substitute to cash and only used when the firm has none.

5. NUMERICAL ANALYSIS OF THE CONTRACT

To illustrate the model, we present numerical examples based on the parameters given in Table [1.](#page-20-0) We follow [Bolton et al.](#page-31-0) [\(2011\)](#page-31-0) in setting r, μ , and λ . We set the liquidation

^{16.} Because secured debt is always repaid in full, the relative security of secured debt claims does not matter. Thus, one could without loss of generality label part of the outstanding secured debt as super senior secured.

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Figure 2

Contract Dynamics. This figure plots $\beta(C)$ and $\alpha(C)$ against C both for $\pi=0.5$ (Panels A and C) and $\pi = 0.01$ (Panels B and D). The parameters follow Table [1.](#page-20-0)

value to $L=1$, which is about 33.3% of the firm's first-best value $\mu/r=3$ in line with the liquidation values of non-financial firms reported in [Kermani and Ma](#page-32-12) [\(2023\)](#page-32-12). We take the intermediary's risk bearing capacity to be $1/\rho = 0.167$, similar to [He](#page-32-13) [\(2011\)](#page-32-13), and normalize $\sigma = 1$, which also normalizes $Y^A = 0$. In the absence of refinancing opportunities, that is, $\pi = 0$, the firm is liquidated at $C = -L$. In the baseline, we pick $\pi = 0.5$ (that is, expected time until the next market access is $1/\pi = 2$ years) leading to $C < -L$ and the firm does not liquidate; we also provide analysis for $\pi = 0.01$ in which case the firm is liquidated at $C = -L$ ^{[17](#page-21-0)} The model's qualitative outcomes are robust to the choice of these parameters.

5.1. Risk-sharing Dynamics

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Figure [2](#page-21-1) illustrates the contract dynamics by plotting $\alpha(C), \alpha_U(C)$, and $\beta(C)$ against C in the state space (\underline{C},C) , both for $\pi=0.5$ (see Panels A and C) and $\pi=0.01$ (see Panels B and D). The boundaries C and \overline{C} are indicated as a vertical blue and red line respectively. In Panels A and C, $\pi=0.5$ and $C^{S}<-L$, so the firm never liquidates and $\lim_{C\to C} \beta(C)=1$. In Panels B and D, for $\pi=0.01$, the firm liquidates at $-L$, with $\beta(\underline{C})$ < 1.

Panels A and B of Figure [2](#page-21-1) show that the intensity of risk-sharing $\beta(C)$ decreases with C or, alternatively, increases with how financially constrained the firm is. Due to financial constraints, shareholders are effectively risk-averse, i.e., $P''(C) < 0$. It is thus optimal to share risk with the intermediary through $\beta(C) > 0$, which is costly due to the intermediary's limited risk-bearing capacity. Because the effective risk aversion

^{17.} Our choice $\pi = 0.5$ follows [Hugonnier et al.](#page-32-1) [\(2015\)](#page-32-1) who assume an arrival rate of market access of 2 and incumbent shareholders' bargaining power of 0.25, resulting in an effective arrival rate of $0.25 \times 2 = 0.5$.

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Figure 3

Boundaries: Comparative statics of the boundaries C, \overline{C} with respect to to the expected time until refinancing $1/\pi$ (top left panel), profitability μ (top right panel), cash flow volatility σ (bottom left panel), intermediary risk aversion ρ (bottom right panel). The parameters follow Table [1.](#page-20-0)

of shareholders decreases in C, while the intermediary's risk-bearing capacity $1/\rho$ is constant, $\beta(C)$ decreases with C.

Panels C and D of Figure [2](#page-21-1) show that, provided [\(14\)](#page-9-1) does not bind, $\alpha(C) = \alpha_U(C)$ smoothly decreases with C. Recall that α can be understood as a costly financing or risk-sharing instrument. Setting $\alpha(C) > 0$ essentially transforms flow payouts to the intermediary today, i.e., from states in which the firm is constrained, into a promised lumpy payout upon refinancing in the future, i.e., a state in which the firm is financially unconstrained. This transfer of promised payments to the future is relatively more beneficial when net liquidity is lower and the firm is more constrained, but exposing the intermediary to the market access shock is costly. The optimal choice of α trades off relaxation of financial constraints now versus larger payments to the intermediary in the future, so unconstrained $\alpha_U(C)$ decreases with C. However, limited liability limits what amount $\alpha(C)$ can be promised, as shown in the constraint [\(14\)](#page-9-1). It is binding when C is low and close to \underline{C} . In this case, $\alpha(C)$ mechanically increases with C, as additional excess liquidity C relaxes the constraint (14) .

5.2. Determinants of Financing Capacity and Utilization

We examine the determinants of the firm's financing and, specifically, when and whether it is cash flow-based or asset-based. Recall that in light of our implementation from Section [4,](#page-14-0) the firm's financing capacity also represents the firm's secured debt capacity.

Figure [3](#page-22-0) plots C and \overline{C} against the expected time to refinancing $1/\pi$ (Panel A), cash flow drift μ (Panel B), cash flow volatility σ (Panel C), and intermediary CARA coefficient ρ (Panel D). Figure [3](#page-22-0) shows that the firm's financing capacity $\overline{Y} = -C$ increases with access to equity financing π , i.e., C increases with $1/\pi$, and the firm's

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cash flow rate μ , while it decreases with cash flow volatility σ and intermediary CARA coefficient ρ (recall that $1/\rho$ is the intermediary's risk-bearing capacity). Thus, financing capacity is cash flow-based for low values of $1/\pi$, σ , ρ or when μ is high. Otherwise financing capacity is asset-based. Intuitively, intermediaries are more willing to provide financing against cash flow for firms with high profitability μ and less volatile cash flows σ. At the same time, low values of µ and large values of σ are associated with larger target cash holdings \overline{C} .^{[18](#page-23-0)}

Related to Corollary [1,](#page-13-2) Panel D of Figure [3](#page-22-0) shows that financing capacity decreases with ρ and is cash flow-based only for low values of ρ , while target cash holdings C increase with ρ . That is, the model predicts that intermediaries with higher risk-bearing capacity are more willing to provide cash flow-based financing, specifically, secured cash flow-based debt.^{[19](#page-23-1)}

As discussed in Section [4.3,](#page-18-1) Panel A shows that lower $1/\pi$ increases financing capacity and reduces the reliance on costly precautionary cash holdings as captured by C by allowing the firm to raise new equity capital more frequently. As shown in the Panel, the better the access to equity financing, the more likely the firm's financing capacity is cash flow-based rather than asset-based, highlighting the dynamic complementarity between debt and equity.

Finally, Figure [4](#page-24-0) illustrates how the firm's average secured debt balance $avg(Y_t)$. the average utilization of secured debt capacity $avg(Y_t/\overline{Y})$, and the average leverage ratio defined as $avg(Leverage_t) = avg\left(\frac{Y_t + \alpha_{U,t}}{P_t + Y_t + \alpha_{U,t}}\right)$ ^{[20](#page-23-2)} change with $1/\pi$ (left column), ρ (middle column), and σ (right column). Observe that these quantities are hump-shaped in $1/\pi$ and σ , in that firms rely the most on (secured) debt when access to equity financing and cash flow volatility take intermediate values.

The intuition for the hump-shaped patterns in Panels A and C is that firms obtain relatively little secured debt and debt in general when (i) their secured debt capacity is high but they do not need it due to low cash flow risk or frequent access to equity financing or (ii) when their secured debt capacity is low. The intuition for this pattern carrying through to secured debt utilization in Panels D and F is more subtle. Firms with low cash flow volatility or easy access to equity financing have high secured debt capacity, but do not need it, explaining the left side of the graphs. In contrast, firms with high cash flow volatility or little access to equity financing try to avoid using secured debt altogether by accumulating greater cash balances before paying dividends, i.e., selfinsuring via cash. Finally, Panels G and I show that the hump-shape in secured-debt usage and utilization extends to overall leverage as well, with similar intuition as above.

Panels B, E, and H show that the firm's reliance on debt financing increases when the intermediary exhibits a higher risk-bearing capacity. The intuition is that when ρ is low, the cost of risk-sharing is low, which enhances access to debt financing in general

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^{18.} More volatile cash flows raise the need for precautionary cash holdings (Décamps et al., [2011\)](#page-31-1). \overline{C} is non-monotone in μ because an increase in μ raises profitability and thus makes liquidation more costly while reducing the need for precautionary cash. The liquidation effect dominates for low μ because financing capacity is asset-based. Otherwise the precautionary saving effect dominates.

^{19.} Different types of intermediaries may exhibit different risk-bearing capacities. Because banks face regulatory capital constraints, they likely have lower risk-bearing capacity. Non-bank lenders face less regulatory constraints than banks but still might be capital-constrained, so they likely have higher risk-bearing capacity.

^{20.} Note that equity is measured at its market value P_t , while debt is measured at its book value $Y_t + \alpha_{U,t}.$

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Debt Financing. This figure plots the average secured debt $avg(Y_t)$ (top row), the average utilization of secured debt capacity $avg(Y_t)/\overline{Y}$ (middle row), and the average leverage $avg(Leverage_t) = avg\left(\frac{Y_t+\alpha_{U,t}}{P_t+Y_t+\alpha_{U,t}}\right)$ (bottom row) against $1/\pi$ (left column), ρ (middle column), and σ (right column). The parameters follow Table [1.](#page-20-0)

and also increases its usage. This effect implies that firms use more secured debt and, specifically, cash flow-based secured debt, when creditors exhibit a higher risk-bearing capacity.

6. EMPIRICAL IMPLICATIONS

In this section, we give an overview of the key empirical implications of our theory. We also explain how these implications are novel and unique to our setting, which combines optimal contracting and dynamic liquidity management.

Before describing these implications in detail, let us briefly discuss the distinction between debt capacity in the model and the empirical measurement for the basis of debt. As discussed in [Lian and Ma](#page-32-0) [\(2021\)](#page-32-0), secured debt can be either asset-based or cash flow-based. Asset-based debt is secured by specific assets, while cash flow-based debt is unsecured or secured by a blanket lien on the firm. For asset-based debt, the final recourse of the creditor is to sell the asset at scrap value, which in our model is the case for $\overline{Y} = L$. For cash flow-based debt, the final recourse of the creditor is to take ownership and sell the firm to new investors, occurring in our model if and only if $\overline{Y} > L$. In particular, when $Y \in (L, \overline{Y})$, part of the firm's secured debt is necessarily cash flowbased, i.e., backed by the firm's going-concern value. Thus, a cash flow-based secured debt capacity \overline{Y} implies the use of cash flow-based secured debt in some states. These observations link the distinction between cash flow-based and asset-based secured debt capacity in our setting to practice.

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Financing Instruments and Secured vs. Unsecured Debt. In our implementation, the firm uses multiple securities to manage liquidity at the same time, leading to an overlapping pecking order. This strategy facilitates state-dependent risk sharing. Outside of distress, the firm uses cash, i.e. retained earnings, and unsecured debt simultaneously. This pattern is supported by the rich interaction between leverage and cash management policies documented in [DeAngelo et al.](#page-31-18) [\(2022\)](#page-31-18) who show that (net of cash) leverage increases as cash balances decrease. The firm uses unsecured debt in all states to share liquidity risk with creditors, consistent with the practice of using credit lines as liquidity management tools (see, e.g., [Acharya et al.](#page-31-19) [2014;](#page-31-19) [Brown et al.](#page-31-20) [2021\)](#page-31-20). The firm also relies on secured debt, but primarily in distress situations, consistent with [Rauh and](#page-32-14) [Sufi](#page-32-14) [\(2010\)](#page-32-14); [Benmelech et al.](#page-31-21) [\(2024,](#page-31-21) [2022\)](#page-31-22).

Our model demonstrates that debt (in general) is not negative cash. When the firm runs out of cash, it needs to issue the most "negative cash"-like security it can. Secured debt fills this role because, in our context, it is the least risky among all debt securities. Therefore, unlike unsecured debt and cash, secured debt and cash act as substitutes. Our model further predicts that the use of unsecured debt allows the firm to issue more secured debt, making unsecured debt and secured debt complements. The mechanism is that unsecured debt absorbs cash flow risk and therefore raises the collateral value of cash flows, thereby allowing secured debt to be cash flow based.

Our predictions about different financing instruments arise from combining dynamic liquidity management with optimal contracting. As a result, unsecured credit lines are optimal for risk-sharing, while secured debt acts as a cash substitute. Endogenous security design is crucial for understanding the use of these instruments. Unlike other models that treat cash as negative debt (see, e.g., [Bolton et al.](#page-31-0) [2011,](#page-31-0) [2021\)](#page-31-2), we show that unsecured debt complements both cash and secured debt, which are substitutes. This explains why firms use different financing tools simultaneously to manage liquidity and optimize risk-sharing.

Debt and Equity as Dynamic Complements. In our model, improved access to equity financing, such as that enjoyed by public firms, increases secured debt capacity and access to cash flow-based debt. This prediction is supported by the finding of [Lian](#page-32-0) [and Ma](#page-32-0) (2021) that public firms use more cash flow-based debt than private firms.^{[21](#page-25-0)} Similarly, private firms backed by Private Equity (PE) funds have better access to equity financing, and thus our model predicts that they can obtain higher leverage compared to otherwise similar firms. This explanation for increased leverage of PE backed firms differs from ones focused on tax benefits or leveraging investments. Further, our analysis suggests that PE-backed firms use more cash flow-based debt than non PE-backed firms, and that PE sponsorship relaxes financing constraints with lenders [\(Ivashina and Kovner,](#page-32-15) [2011;](#page-32-15) [Demiroglu and James,](#page-31-23) [2010\)](#page-31-23).

These empirical predictions rest upon a key insight from our model: Creditors are willing to offer cash flow-based debt because they anticipate that the firm will survive long enough to locate new equity investors. At the same time, the firm is only able to survive long enough because it can obtain cash flow-based debt. Improved access to equity financing strengthens this feedback effect, thereby raising secured debt capacity and facilitating access to cash flow-based debt. This mechanism requires a fully

^{21.} Such cash flow-based debt is often secured by a blanket lien, i.e., a security interest in the firm's going concern value minus assets separately pledged in other secured debt contracts.

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dynamic model in which the firms future prospects, i.e., continuation or liquidation, are endogenous to the contract.

Bankruptcy. Our model offers a novel perspective on bankruptcy by showing how it emerges as a tool for optimal risk sharing. Rather than an immediate change in ownership or liquidation, bankruptcy is a process that dynamically resolves either through continuation and reorganization (Chapter 11) or liquidation (Chapter 7). In particular, this process involves allocating all risk to shareholders through dilution and to unsecured creditors through debt default. This approach protects secured creditors and ultimately facilitates debtor-in-possession financing, i.e., the use of senior-secured debt in Chapter 11 bankruptcy, allowing the firm to continue operations during bankruptcy.

In line with distress resolution in our model, [Ivashina et al.](#page-32-16) [\(2016\)](#page-32-16) document that bankruptcy commonly involves the write-down of subordinate debt and equity claims. Further, our model predicts that distress resolution akin to Chapter 11 bankruptcy and debtor-in-possession financing become more prevalent when the firm has better access to equity financing. For private firms, the anticipation of equity injections from PE sponsors raises the creditors' willingness to provide secured debt, specifically, cash flowbased secured debt, which allows the firm to continue operations when in distress and in bankruptcy. This effect implies that PE-backed firms are less likely to be liquidated in distress, as documented in [Hotchkiss et al.](#page-32-17) [\(2021\)](#page-32-17).

By jointly determining the financing constraint and distress resolution, our model highlights an endogenous link between modes of financing and bankruptcy. When creditors anticipate that distress is resolved without liquidation, they are willing to lend against cash flows, enhancing the firm's secured debt capacity. This allows the firm to obtain secured debt to continue operations in bankruptcy, which ultimately prevents liquidation. Thus, cash flow-based financing is tied to the distress resolution via Chapter 11 reorganization, while asset-based financing is linked to distress resolution via both Chapter 11 reorganization and Chapter 7 liquidation. This rationalizes the empirical findings in [Lian and Ma](#page-32-0) [\(2021\)](#page-32-0) that cash flow–based lending is more prevalent in countries with Chapter 11–type corporate bankruptcy systems.

7. EXTENSIONS

7.1. Refinancing and Weak Creditor Rights

Recall that constraint [\(14\)](#page-9-1) implies that the shareholders' continuation payoff is always non-negative by limiting the amount α that can be promised to the intermediary upon refinancing. However, there are states C in which existing shareholders are so heavily diluted upon refinancing that they are worse off than "just before" refinancing, i.e., $J(C)₀$.

For $\nu \in [0,1]$, consider the following generalized constraint on α that nests our base case:

$$
\alpha(C) \le [P(\overline{C}) - \overline{C}] - [(1-\nu)P(C) - C] \iff J(C) \ge -\nu P(C). \tag{33}
$$

Here, $\nu = 1$ yields our baseline constraint [\(14\)](#page-9-1) implying full commitment, while $\nu =$ 0 yields a tighter constraint we term monotonicity, as refinancing cannot make current shareholders worse off via dilution. Thus, ν describes shareholders' strength of commitment to refinance. The solution of this model variant follows the baseline solution, except that constraint (14) is replaced by constraint (33) . The boundary conditions remain the same, specifically the expressions for the lower bound (24) , as

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Contract Dynamics under limited creditor protection. This figure plots $\beta(C)$ and $\alpha(C)$ against C both for $\pi = 0.5$ (Panels A and C) and $\pi = 0$ (Panels B and D). The parameters follow Table [1](#page-20-0) and $\nu = 0$ in refinancing constraint [\(33\)](#page-26-1).

due to $P(C)=0$, we have $J(C)=0$ regardless of ν . The following proposition shows that weaker commitment, i.e., smaller ν , increases the payout boundary and lowers cash flow-based financing capacity.

Proposition 4. The payout boundary \overline{C} and lower boundary under continuation C^{S} both decrease in ν.

Notably, the solution, implementation, and the key results for $\nu < 1$ remain qualitatively similar to the baseline. Figure [5](#page-27-0) illustrates the dynamics of the optimal contract under $\nu = 0$ using the same parameters as in Figure [2.](#page-21-1) The outcomes in Figure [5](#page-27-0) are broadly similar to Figure [2,](#page-21-1) with the differences being that the constraint [\(33\)](#page-26-1) now binds for all C and that C and \overline{C} are larger than in the baseline case.

Our implementation from Proposition [3](#page-14-2) and Corollary [2](#page-18-2) via secured and unsecured debt applies after a change to the interest rate on $d\alpha_U(C)$ and the bankruptcy rules for $\nu < 1.22$ $\nu < 1.22$ The key difference to our baseline implementation is that for $\nu < 1$, existing shareholders are not fully wiped out when creditors take a loss. In other words, APR

22. By (??), the interest rate on the unsecured credit line changes as $\alpha_C(C)$ is redefined by [\(33\)](#page-26-1), so that

$$
d\alpha_U(C) = \left[\frac{\lambda}{\rho r} \mathbb{1}_{\{C \ge 0\}} + \pi (1 - \nu) \left(\frac{e^{\rho r [\alpha_U(C) - \alpha(C)]} - 1}{\rho r}\right)\right] dt - dI^{\alpha_U}(C) - [\alpha_U(C) - \alpha(C)]d\Pi. \tag{34}
$$

Note that the term involving ν , i.e., the second term in [·], is always positive. The unsecured interest rate is positive to compensate the unsecured creditors for the higher expected losses $\alpha_U(C) - \alpha(C)$ from bankruptcy.

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Figure 6

Intermediary Incentives. The left panel of this figure plots the intermediary's effort $a = \beta/\kappa$ both for $\pi = 0.5$ (solid black line) and for $\pi = 0$ (dotted red line) in the transformed state space against $(C-\underline{C})/\overline{(C}-\underline{C})$. The right panel plots average effort $avg(a_t)$ against $1/\pi$. The parameters follow Table [1,](#page-20-0) and we use $\kappa = 10$.

may fail in bankruptcy, and we thus interpret ν as a proxy for creditor protection. In sum, weak creditor protection — which limits the extent of dilution of equity in distress resolution — limits the availability and feasibility of cash flow-based secured debt.

Weaker creditor rights, i.e., lower ν , lead to a decrease in financing capacity, a shift from cash flow-based financing toward asset-based financing, and a shift from Chapter 11 bankruptcy with reorganization toward Chapter 7 bankruptcy and liquidation for distress resolution. Consistent with these predictions, [Antill](#page-31-24) [\(2022\)](#page-31-24) documents that weakened creditor protection is associated with inefficient liquidation in bankruptcy.

7.2. Active Intermediaries and Monitoring

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Financial intermediaries, such as banks or direct lenders, often monitor borrowers to contain credit risk and improve operational performance, or actively engage in financial distress resolution. We extend our model to account for such intermediary actions by allowing the intermediary to affect cash flows via effort. The intermediary's incentives to exert effort increase with the its exposure to cash flow shocks ("skin-in-the-game") β_t .

As described in Online Appendix C.1, we now assume that cash flows evolve according to

$$
dX_t = (\mu + a_t)dt + \sigma dZ_t,\tag{35}
$$

where $a_t \geq 0$ is the intermediary's non-contractible and privately observable effort which entails a cost $\frac{\kappa a_t^2}{2}dt$ for a constant $\kappa > 0.23$ $\kappa > 0.23$ Effort boosts the firm's cash flow drift, which could capture the intermediary's active role in firm operations or its role in disciplining management through monitoring. The intermediary's incentives to exert effort are determined by the incentive condition $a_t = \frac{\beta_t}{\kappa}$, and thus increase with the intermediary's exposure to cash flow shocks β_t . That is, there is a moral hazard with regard to intermediary's monitoring effort.

Panel A of Figure [6](#page-28-1) illustrates the dynamics of effort a in two scenarios, (i) $\pi = 0.5$ in which case $\underline{C} = C^S$ and the firm is never liquidated and (ii) $\pi = 0$ in which case the

^{23.} Note that an infinite cost of effort, i.e., $\kappa \to \infty$, implies $a_t = 0$, thus giving our baseline case.

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firm is liquidated once $C = -L^{24}$ $C = -L^{24}$ $C = -L^{24}$ Intermediary effort increases upon negative cash flow shocks and is highest when C is low. The intermediary exerts particularly high effort when $\beta(C) \approx 1$, which occurs at $C = C$ in the case of cash flow-based financing. Thus, cash flow-based financing is associated with more intense monitoring under financial distress.

Panel B of Figure [6](#page-28-1) plots the intermediary's average effort against $1/\pi$, the expected time to refinancing. Better access to equity markets reduces the intermediary's incentives to monitor, so that $avg(a_t)$ increases with $1/\pi$. That is, that lenders monitor less when borrowers have better access to equity financing. On the contrary, when liquidity dries up, e.g., in a financial crisis, intermediaries providing debt financing exert more effort to improve firm operations or, similarly, engage more in monitoring.

Finally, cash flow-based financing capacity generally decreases with κ and so increases with the intermediary's monitoring ability. Intuitively, when the intermediary can add value to the firm through monitoring, it has a higher valuation for the firm and so is more willing to provide cash flow-based financing.

8. CONCLUSION

We develop a dynamic contracting theory of asset- and cash flow-based financing that demonstrates how firm, intermediary, and capital market characteristics jointly shape firms' financing constraints. A firm with imperfect access to equity financing covers financing needs through costly sources: an intermediary and retained cash. The firm's financing capacity is endogenously determined by either the liquidation value of assets (asset-based) or the intermediary's going-concern valuation of the firm's cash flows (cash flow-based). The optimal contract is implemented with defaultable debt — specifically an unsecured credit line and senior-secured debt — and features optimal risk-sharing via bankruptcy. When the firm does well, it repays its debt in full. When it does poorly, distress resolution mirrors U.S. bankruptcy procedures (Chapter 7 vs 11). Secured and unsecured debt are complements because risk-sharing via unsecured debt increases secured debt capacity. Debt and equity are dynamic complements because access to equity financing increases debt capacity.

By providing a micro-foundation of financing constraints through the lens of dynamic contracting theory, our paper can provide guidance on reduced-form financing constraints, for instance, in dynamic macroeconomic models. While most papers in the macroeconomic literature focus on collateral, i.e., asset-based, constraints as key financing constraint [\(Kiyotaki and Moore,](#page-32-18) [1997;](#page-32-18) [Bernanke et al.,](#page-31-25) [1999;](#page-31-25) Dávila and [Korinek,](#page-31-26) [2018\)](#page-31-26), [Greenwald](#page-32-19) [\(2019\)](#page-32-19), [Drechsel and Kim](#page-32-20) [\(2022\)](#page-32-20), and [Drechsel](#page-31-27) [\(2023\)](#page-31-27) introduce cash flow-based financing constraints in general equilibrium models. Our findings provide guidance how these constraints are related to capital market and intermediary characteristics.

A. SUMMARY OF VARIABLES USED IN MODEL AND NOTATION

In Table [A1](#page-20-0) we provide a summary of the variables and notation used in the model.

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24. To facilitate comparison across scenarios, we plot intermediary effort a against the adjusted liquidity position $(C-C)/(\overline{C}-C) \in [0,1]$ both for $\pi=0.5$ (solid black line) and for $\pi=0$ (dotted red line).

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Variable definitions. See Table [1](#page-20-0) for parameter definitions.

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Supplementary Data

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[Supplementary data](#page-0-0) are available at *Review of Economic Studies* online and contains the proofs for all of our results.

Data Availability Statement

The code used to conduct the numerical analysis in this article is available on Zenodo at [https://doi.](https://doi.org/10.5281/zenodo.13916906) [org/10.5281/zenodo.13916906](https://doi.org/10.5281/zenodo.13916906).

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